## Energy Efficient Algorithms Assignment 2

Hand in on Monday, June 2, 2008, during the lecture.

Exercise 1: Idle periods governed by probability distribution. Determine the best deterministic algorithm  $A_{\mathcal{Q}}^*$  for the probability distribution  $\mathcal{Q} = (q_T)_{0 \leq T < \infty}$  on the length of idle periods that is given by

$$q_T = e^{-T}.$$

**Exercise 2: Transition points in a multiple-state system.** Remember the optimal (offline) power-down strategy in a multiple-state system. Let  $S = (s_0, \ldots, s_l)$  be the sequence of possible states ordered by decreasing energy consumption  $(s_0$  is the active state), let S(t) denote the optimal state at time t, and let  $b_i$  denote the first time instant at which  $s_i$  becomes the optimal state. So  $b_0 = 0$  and for  $0 < i \leq l$ :

$$D(i-1) + r_{i-1}b_i = D(i) + r_ib_i$$

where  $D(i) = d_{0,i}$  is the transition cost to move from  $s_0$  to  $s_i$ , and  $r_i$  is the power consumption rate in state  $s_i$ .

Provided that the optimal strategy will use every state, i.e.  $range(S(t)) = \{s_0, \ldots, s_l\}$ , show that the sequence of the  $b_i$  is increasing:

$$b_0 < b_1 < \ldots < b_l$$
.

Exercise 3: Multiple-state system with additive power-down costs. Consider a multiple-state system where the energy used in transitioning down is additive. That is, for  $0 \le i < k < j \le l$ :

$$d_{ij} = d_{ik} + d_{kj}.$$

Show that in this scenario, algorithm ALG from the lecture is 2-competitive.

*Hints:* Since the worst case occurs at  $t = b_i$  for some  $0 < i \leq l$ , you can focus on this case when estimating the ratio ALG(t)/OPT(t). Also observe that  $OPT(b_i) \geq D(i)$ . An assumption of the form  $D(i) \geq \gamma D(i-1)$  is not necessary here.

**Exercise 4: Investigation of a multiple state system.** For a system with multiple power saving states of your choice (e.g. your own laptop in particular or the ACPI standard in general), read up on its characteristics. Report on your findings concerning for example the field of application, the number of states, the corresponding energy consumptions, transition times and transition costs, etc.