

Network Algorithms

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**Lecture notes to a large part by Roger Wattenhofer, ETH Zurich
(for the course “Principles of Distributed Computing”)**

Introduction

What is Distributed Computing?

In the last few decades, we have experienced an unprecedented growth in the area of distributed systems and networks. Distributed computing now encompasses many of the activities occurring in today's computer and communications world. Indeed, distributed computing appears in quite diverse application areas: The Internet, wireless communication, cloud or parallel computing, multi-core systems, mobile networks, but also an ant colony, a brain, or even the human society can be modeled as distributed systems.

These applications have in common that many processors or entities (often called nodes) are active in the system at any moment. The nodes have certain degrees of freedom: they have their own hard- and software. Nevertheless, the nodes may share common resources and information, and, in order to solve a problem that concerns several—or maybe even all—nodes, coordination is necessary.

Despite these commonalities, a human brain is of course very different from a quadcore processor. Due to such differences, many different models and parameters are studied in the area of distributed computing. In some systems the nodes operate synchronously, in other systems they operate asynchronously. There are simple homogeneous systems, and heterogeneous systems where different types of nodes, potentially with different capabilities, objectives etc., need to interact. There are different communication techniques: nodes may communicate by exchanging messages, or by means of shared memory. Occasionally the communication infrastructure is tailor-made for an application, sometimes one has to work with any given infrastructure. The nodes in a system often work together to solve a global task, occasionally the nodes are autonomous agents that have their own agenda and compete for common resources. Sometimes the nodes can be assumed to work correctly, at times they may exhibit failures. In contrast to a single-node system, distributed systems may still function correctly despite failures as other nodes can take over the work of the failed nodes. There are different kinds of failures that can be considered: nodes may just crash, or they might exhibit an arbitrary, erroneous behavior, maybe even to a degree where it cannot be distinguished from malicious (also known as Byzantine) behavior. It is also possible that the nodes follow the rules indeed, however they tweak the parameters to get the most out of the system; in other words, the nodes act selfishly.

Apparently, there are many models (and even more combinations of models) that can be studied. We will not discuss them in detail now, but simply define

them when we use them. Towards the end of the course a general picture should emerge, hopefully!

Course Overview

This course introduces the basic principles of distributed computing, highlighting common themes and techniques. In particular, we study some of the fundamental issues underlying the design of distributed systems:

- **Communication:** Communication does not come for free; often communication cost dominates the cost of local processing or storage. Sometimes we even assume that everything but communication is free.
- **Coordination:** How can you coordinate a distributed system so that it performs some task efficiently? How much overhead is inevitable?
- **Fault-tolerance:** A major advantage of a distributed system is that even in the presence of failures the system as a whole may survive.
- **Locality:** Networks keep growing. Luckily, global information is not always needed to solve a task, often it is sufficient if nodes talk to their neighbors. In this course, we will address whether a local solution is possible.
- **Parallelism:** How fast can you solve a task if you increase your computational power, e.g., by increasing the number of nodes that can share the workload? How much parallelism is possible for a given problem?
- **Symmetry breaking:** Sometimes some nodes need to be selected to orchestrate computation or communication. This is achieved by a technique called symmetry breaking.
- **Synchronization:** How can you implement a synchronous algorithm in an asynchronous environment?
- **Uncertainty:** If we need to agree on a single term that fittingly describes this course, it is probably “uncertainty”. As the whole system is distributed, the nodes cannot know what other nodes are doing at this exact moment, and the nodes are required to solve the tasks at hand despite the lack of global knowledge.

Finally, there are also a few areas that we will not cover in this course, mostly because these topics have become so important that they deserve their own courses. Examples for such topics are distributed programming or security/cryptography.

In summary, in this class we explore essential algorithmic ideas and lower bound techniques, basically the “pearls” of distributed computing and network algorithms. We will cover a fresh topic every week.

Have fun!

Chapter Notes

Many excellent text books have been written on the subject. The book closest to this course is by David Peleg [Pel00], as it shares about half of the material. A main focus of Peleg's book are network partitions, covers, decompositions, spanners, and labeling schemes, an interesting area that we will only touch in this course. There exist a multitude of other text books that overlap with one or two chapters of this course, e.g., [Lei92, Bar96, Lyn96, Tel01, AW04, HKP⁺05, CLRS09, Suo12]. Another related course is by James Aspnes [Asp] and one by Jukka Suomela [Suo14].

Most chapters of this course have been written by Roger Wattenhofer from ETH Zurich. Some of these chapters have been developed in collaboration with (former) Ph.D. students of Roger Wattenhofer, see chapter notes for details. Many students have helped to improve exercises and script. Thanks go to Philipp Brandes, Raphael Eidenbenz, Roland Flury, Klaus-Tycho Förster, Stephan Holzer, Barbara Keller, Christoph Lenzen, Thomas Locher, Remo Meier, Thomas Moscibroda, Regina O'Dell, Yvonne-Anne Pignolet, Jochen Seidel, Stefan Schmid, Johannes Schneider, Jara Uitto, Pascal von Rickenbach (in alphabetical order).

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