Albert-Ludwigs-Universität, Inst. für Informatik
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Theoretical Computer Science - Bridging Course
Summer Term 2018
Exercise Sheet 4

for getting feedback submit electronically by 06:00 am, Monday, May 28th, 2018

Exercise 1: Context-Free Grammar   *(3+2 Points)*

For each of the following languages, give a context-free grammar to accept the language.

(a) $L_1 = \{w \# w' | w^R$ is a substring of w', and $w, w' \in \{0, 1\}^*\}$. [1]

(b) $L_2 = \{0^i 1^j 2^k | i \neq j$ or $j \neq k\}$

Exercise 2: Chomsky Normal Form   *(5 Points)*

Consider the following context-free grammar (CFG):

$$S \rightarrow aSb \mid D$$
$$D \rightarrow ccDcc \mid \varepsilon$$

Convert this CFG into an equivalent one in Chomsky Normal Form. Give the grammar you obtained after each step of the conversion algorithm.

Exercise 3: Constructing Pushdown Automata   *(4 Points)*

Consider the language $L = \{a^n b^{2m} b a^n \mid m, n > 0\}$ over the alphabet $\Sigma = \{a, b\}$.
Construct a PDA $\mathcal{A}$ with $L(\mathcal{A}) = L$.

Exercise 4: Pumping Lemma for Context-Free Languages *(3+3 Points)*

Use the pumping lemma to show that the following languages over the alphabet $\Sigma = \{a, b\}$ are not context free:

(a) $\{ww \mid w \in \{a, b\}^*\}$

(b) $\{a^n b a^{2n} b a^{3n} \mid n \geq 0\}$

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[1] w^R is achieved by reversing the order of the symbols in w.