



# Chapter 4 Causality, Time, and Global States

**Distributed Systems** 

**SS 2019** 

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# Time in Distributed Systems



Goal: Establish a notion of time in (partially) asynchronous systems

#### Physical time:

- Establish an approximation of real time in a network
- Synchronize local clocks in a network
- Timestamp events (email, sensor data, file access times etc.)
- Synchronize audio and video streams
- Measure signal propagation delays (Localization)
- Wireless (TDMA, duty cycling)
- Digital control systems (ESP, airplane autopilot etc.)

#### Logical time:

- Determine an order on the events in a distributed system
- Establish a global view on the system

# **Logical Clocks**



**Goal:** Assign a timestamp to all events in an asynchronous message-passing system

- Allows to give the nodes some notion of time
  - which can be used by algorithms
- Logical clock values: numerical values that increase over time and which are consistent with the observable behavior of the system
- The objective here is not to do clock synchronization:
  - **Clock Synchronization:** compute logical clocks at all nodes which simulate real time and which are tightly synchronized.
    - We will briefly talk about clock synchronization later...

# Observable Behavior



#### **Recall Executions / Schedules**

- An exec. is an alternating sequence of configurations and events
- A schedule S is the sequence of events of an execution
  - Possibly including node inputs
- Schedule restriction for node v:

$$S|v :=$$
 "sequence of events seen by  $v$ "

#### **Causal Shuffles**

We say that a schedule  $\underline{S}'$  is a **causal shuffle** of schedule  $\underline{S}$  iff

$$\forall v \in V: \ \underline{S|v} = \underline{S'|v}$$

**Observation:** If S' is a causal shuffle of S, no node/process can distinguish between S and S'.

# Causal Order



Logical clocks are based on a causal order of the events

- In the order, event e should occur before event e' if event e provably occurs before event e'
  - In that case, the clock value of e should be smaller than the one of e'

#### For a given schedule S:

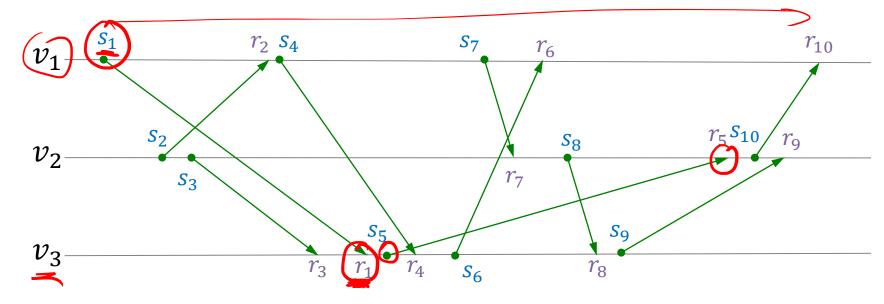
- The distributed system cannot distinguish S from another schedule S' if and only if S' is a causal shuffle of S.
  - − causal shuffle ⇒ no node can distinguish
  - no causal shuffle  $\Rightarrow$  some node can distinguish

Event  $\underline{e}$  provably occurs before  $\underline{e}'$  if and only if  $\underline{e}$  appears before  $\underline{e}'$  in all causal shuffles of S

# Causal Shuffles / Causal Order Example

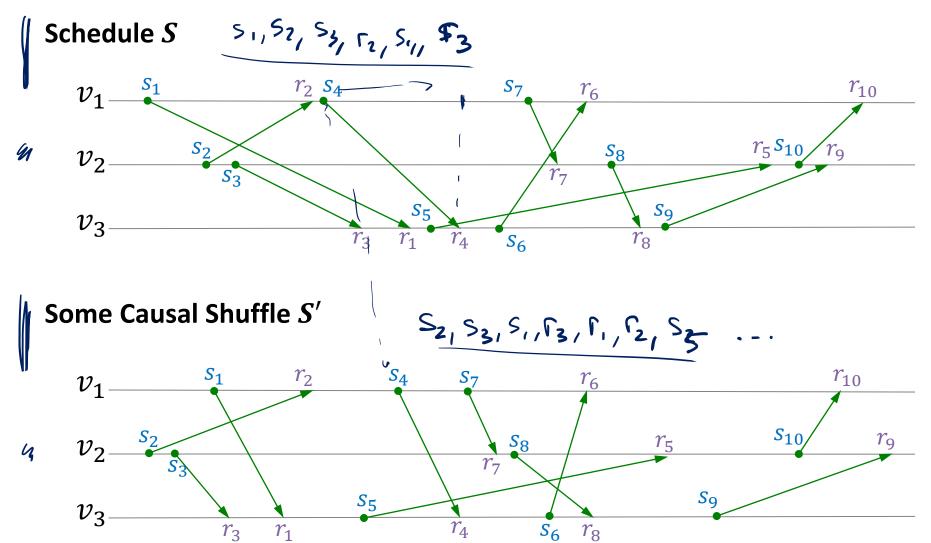


#### Schedule S



# Causal Shuffles / Causal Order Example





# Lamport's Happens-Before Relation



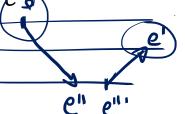
**Assumption:** message passing system, only <u>sen</u>d and <u>receive</u> events

# Consider two events $\underline{e}$ and $\underline{e}'$ occurring at nodes $\underline{u}$ and $\underline{u}'$

- send event occurs at sending node, recv. event at receiving node
- let's define  $\underline{t}$  and  $\underline{t}'$  be the (real) times when e and e' occur

# We know that e provably occurs before e' if

- 1. The events occur at the same node and e occurs before e'
- 2. Event e is a send event, e' the recv. event of the same message
- 3. There is an event e'' for which we know that provably, e occurs before e'' and e'' occurs before e''



# Lamport's Happens-Before Relation



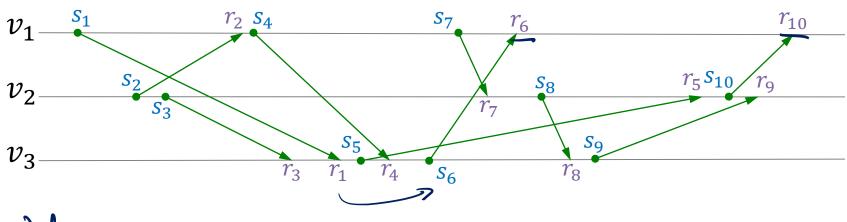
**Definition:** The happens-before relation  $\Rightarrow_S$  on a schedule S is a pairwise relation on the send/receive events of S and it contains

- 1. All pairs  $(\underline{e}, \underline{e}')$  where  $\underline{e}$  precedes  $\underline{e}'$  in  $\underline{S}$  and  $\underline{e}$  and  $\underline{e}'$  are events of the same node/process.
- 2. All pairs (e, e') where e is a send event and e' the receive event for the same message.
- 3. All pairs (e,e') where there is a third event e'' such that  $e \Rightarrow_S e'' \land e'' \Rightarrow_S e'$ 
  - Hence, we take the transitive closure of the relation defined by 1. and 2.

# Happens-Before Relation: Example



#### Schedule S



$$\forall i: S_i \Rightarrow_S \Gamma_i$$

$$S_i \Rightarrow_S \Gamma_i \Rightarrow_S S_6, S_6 \Rightarrow_S \Gamma_6, \Gamma_6 \Rightarrow_S \Gamma_{10}$$

$$S_i \Rightarrow_S \Gamma_{10}$$



**Theorem:** For a schedule S and two (send and/or receive) events e and e', the following two statements are equivalent:

- a) Event e happens-before e', i.e.,  $e \Rightarrow_S e'$ .  $\neg (e \Rightarrow_S e')$ b) Event e precedes e' in all causal shuffles S' of S.  $\neg (e' \Rightarrow_S e')$

#### Some remarks before proving the theorem...

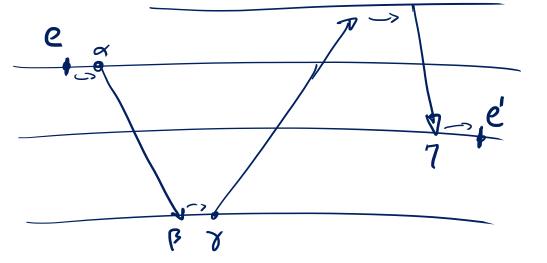
- Shows that the happens-before relation is exactly capturing what we need about the causality between events
  - It captures exactly what is observable about the order of events
- To prove the theorem, we show that
  - 1. a)  $\rightarrow$  b)
  - 2. b)  $\rightarrow$  a)



 $\underline{\mathsf{lf}\ e \Rightarrow_S e'}$ , then  $\underline{e}$  precedes  $\underline{e'}$  in all causal shuffles S' of S.

- 1) e, e' occur at the same node
- -2) e,e' belong to the same usg. (e: send, e': receive)
  - 3)

<u>S:</u>





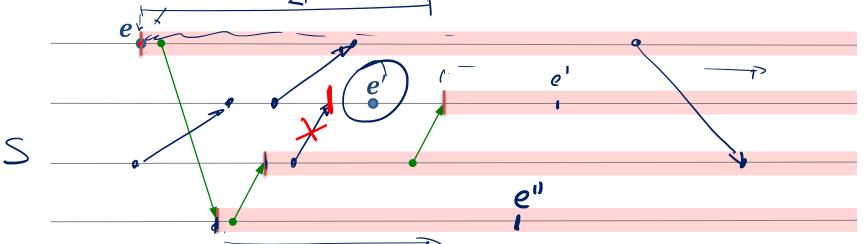
If e precedes e' in all causal shuffles S' of S, then  $e \Rightarrow_S e'$ .

#### **Proof:**





- Show:  $e \not\Rightarrow_S e'$  there is a shuffle S' such that e' precedes e in S
- W.l.o.g., assume that e precedes e' in S
  - Consequently, e and e' happen at different nodes (otherwise, the order remains the same in all causal shuffles)



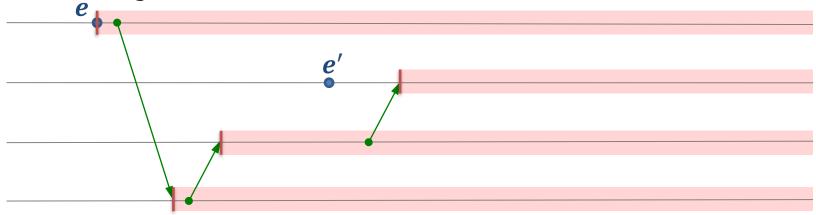
Events in red part can be shifted by fixed amount  $\Delta$ 



If e precedes e' in all causal shuffles S' of S, then  $e \Rightarrow_S e'$ .

#### **Proof:**

• Show:  $e \not\Rightarrow_S e'$ , there is a shuffle S' such that e' precedes e in S



# Events in red part can be shifted by fixed amount Δ

- Consider some message M with send/receive events  $s_M$ ,  $r_M$
- If  $s_M$  and  $r_M$  or only  $r_M$  are shifted, message delay gets larger  $\rightarrow$  OK
- It is not possible to only shift  $s_M$
- Choose  $\Delta$  large enough to move e past e'

# **Lamport Clocks**



#### **Basic Idea:**

- 1. Each event e gets a clock value  $\underline{\tau(e)} \in \mathbb{N}$
- 2. If e and e' are events at the same node and e precedes e', then  $\tau(e) < \tau(e')$
- 3. If  $s_M$  and  $r_M$  are the send and receive events of some msg. M,  $\tau(s_M) < \tau(r_M)$

#### **Observation:**

• For clock values  $\tau(e)$  of events e satisfying 1., 2., and 3., we have

$$e \Rightarrow_{S} e' \longrightarrow \underline{\tau(e)} < \tau(e')$$

- because < relation (on  $\mathbb{N}$ ) is transitive
- Hence, the partial order defined by  $\tau(e)$  is a superset of  $\Rightarrow_s$

# **Lamport Clocks**



#### Algorithm:

- Each node u keeps a counter  $\underline{c_u}$  which is initialized to  $\underline{0}$
- For any non-receive event e at node u, node u computes

$$c_u \coloneqq c_u + 1; \ \tau(e) \coloneqq c_u$$

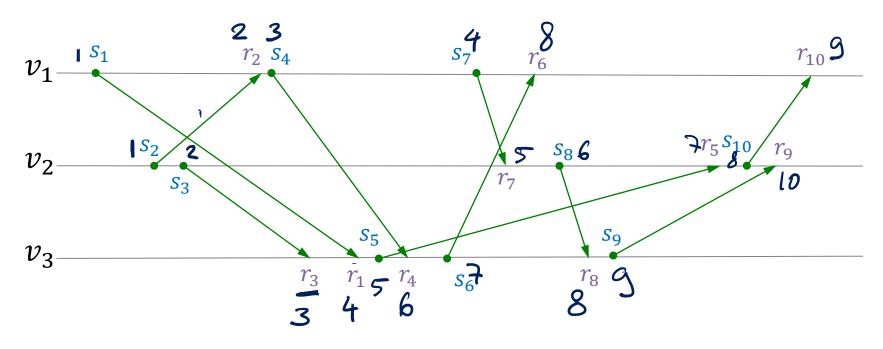
- For any send event s at node u, node u attaches the value of  $\tau(s)$  to the message
- For any receive event r at node u (with corresponding send event s), node u computes

$$c_u \coloneqq \max\{c_u, \underline{\tau(s)}\} + 1; \ \tau(r) \coloneqq c_u$$

# Lamport Clocks: Example



#### Schedule S



# Neiger-Toueg-Welch Clocks



#### **Discussion Lamport Clocks:**

- Advantage: no changes in the behavior of the underlying protocol
- Disadvantage: clocks might make huge jumps (when recv. a msg.)

#### Idea by Neiger, Toueg, and Welch:

- Assume nodes have some approximate knowledge of real time
  - e.g., by using a clock synchronization algorithm
- Nodes increase their clock value periodically
- Combine with Lamport clock ideas to ensure safety
- When receiving a message with a time stamp which is larger than the current local clock value, wait with processing the message.

# Fidge-Mattern Vector Clocks



- Lamport clocks give a superset of the happens-before relation
- Can we compute logical clocks to get ⇒<sub>S</sub> exactly?

#### **Vector Clocks:**

- Each node u maintains an vector VC(u) of clock values
  - one entry VC<sub>v</sub>(u) for each node v ∈ V
- In the vector VC(e) assigned (by u) to some event e happening at node u, the component  $x_v$  corresponding to  $v \in V$  refers to the

number of events at node  $oldsymbol{v}$ ,  $oldsymbol{u}$  knows about when  $oldsymbol{e}$  occurs

# **Vector Clocks Algorithm**



- All Nodes u keep a vector VC(u) with an entry for all nodes in V
  - all components are initialized to 0
  - component corresponding to node  $v: VC_v(u)$
- For any non-receive event e at node u, node u computes

$$VC_u(u) := VC_u(u) + 1$$
;  $VC(e) := VC(u)$ 

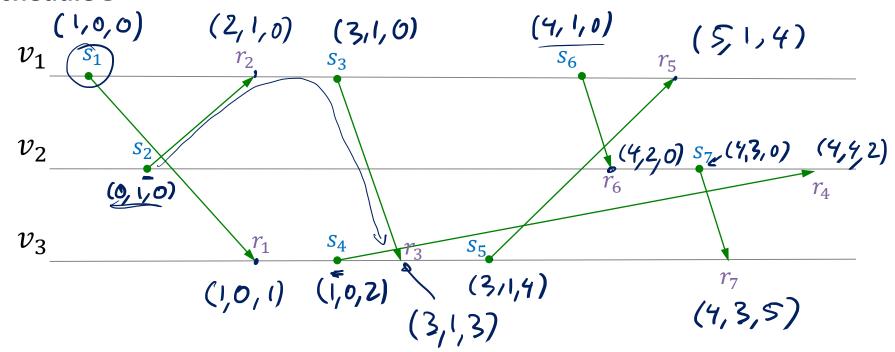
- For any send event s at node u, node u attaches the value of VC(s) to the message
- For any receive event r at node u (with corresponding send event s), node u computes

$$\forall v \neq u : \underline{VC_v(u)} := \max\{\underline{VC_v(s)}, \underline{VC_v(u)}\};$$
  
 $VC_u(u) := \underline{VC_u(u)} + 1;$   
 $VC(r) := \underline{VC(u)}$ 

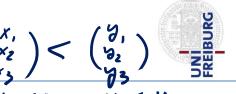
# **Vector Clocks Example**



#### Schedule S

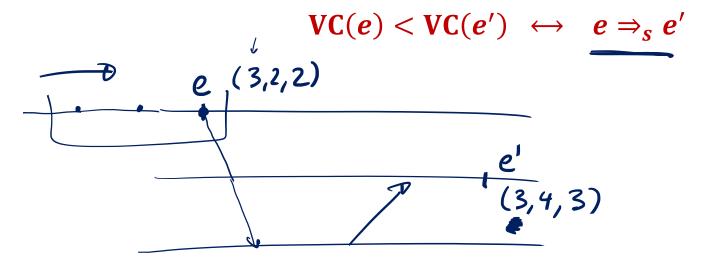


# Vector Clocks and Happens-Before $\binom{x_i}{x_2} < \binom{y_i}{y_3}$



Definition: 
$$VC(e) < VC(e') := (\forall v \in V: VC_v(e) \leq VC_v(e')) \land (VC(e) \neq VC(e'))$$

**Theorem:** Given a schedule S, for any two events e and e',

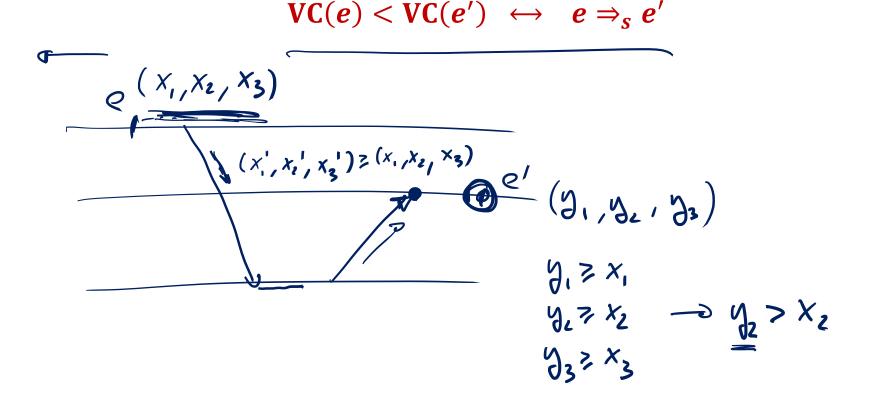


# Vector Clocks and Happens-Before



Definition: 
$$VC(e) < VC(e') :=$$
  $(\forall v \in V: VC_v(e) \leq VC_v(e')) \land (VC(e) \neq VC(e'))$ 

**Theorem:** Given a schedule S, for any two events e and e',



# Logical Clocks vs. Synchronizers



#### **Synchronizer:**

- Algorithm that generates clock pulses that allow to run an synchronous algorithm in an asynchronous network
  - We will discuss synchronizers later

# The clock pulses (local round numbers) generated by a synchronizer can also used as logical clocks

- Send events of round r get clock value 2r-1
- Receive events of round r get clock value 2r
- superset of the happens-before relation
- requires to drastically change the protocol and its behavior
  - synchronizer determines when messages can be sent
- a very heavy-weight method to get logical clock values
  - requires a lot of messages

# **Application of Logical Times**



#### **Replicated State Machine**

- main application suggested by Lamport in his original paper
- a shared state machine where every node can issue operations
- state machine is simulated by several replicas

#### **Solution:**

- add current clock value (and issuer node ID) to every operation
- operations have to be carried out in order of clock values / IDs

#### Safety:

- all replicas use same order of operations
- order of operations is a possible actual order (consistent with local views)

#### Liveness:

progress is guaranteed if nodes regularly send messages to each other

# **Global States**



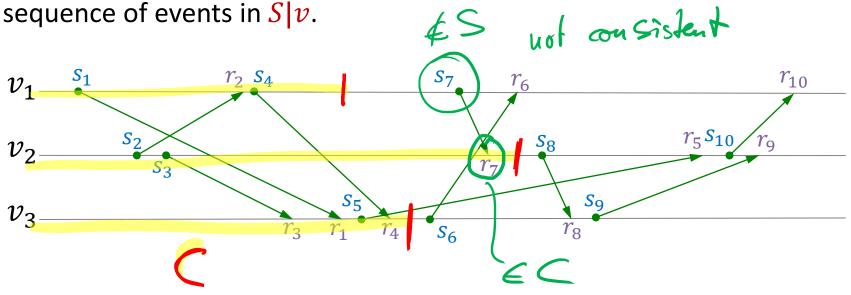
- Sometimes the nodes of a distributed system need to figure out the global state of the system
  - e.g., to find out if some property about the system state is true
- Executions/schedules which lead to the same happens-before relation (i.e., causal shifts) cannot be distinguished by the system.
- Generally not possible to record the global state at any given time of the execution
- Best solution: A global state which is consistent with all local views
  - i.e., a state which could have been true at some time
- Called a consistent or global snapshot of the system and based on consistent cuts of the schedule

# **Consistent Cut**



#### Cut

Given a schedule S, a cut is a subset C of the events of S such that for all nodes  $v \in V$ , the events in C happening at v form a prefix of the

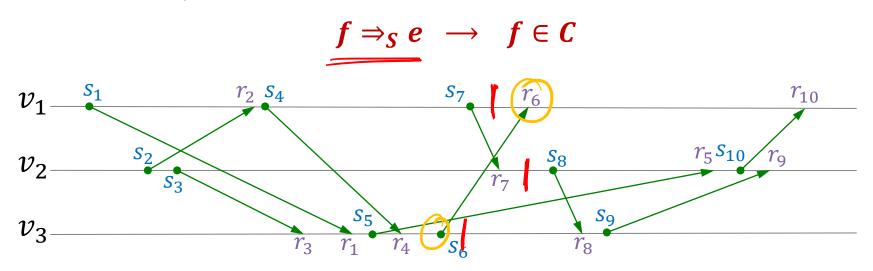


# **Consistent Cut**



#### **Consistent Cut**

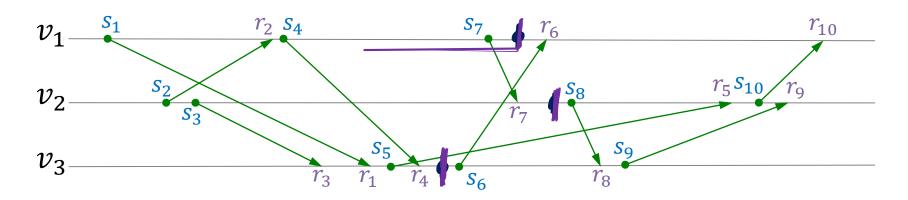
Given a schedule S, a consistent cut C is cut such that for all events  $e \in C$  and all events f in S, it holds that



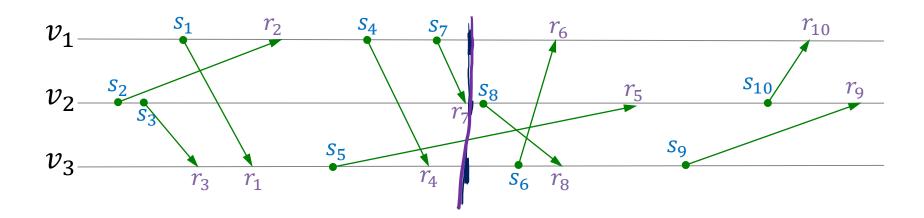
# **Consistent Cut**



# Schedule S



#### Some Causal Shuffle S'



# **Consistent Cuts**



**Claim:** Given a schedule S, a cut C is a consistent cut if and only if for each message M with send event  $s_M$  and receive event  $r_M$ , if  $r_M \in C$ , then it also holds that  $s_M \in C$ .

def. of consistat (uds AN: LEC etter dir. (->) assume C not consis-€ ⇒ € 

# **Consistent Snapshot**



#### **Consistent Snapshot = Global Snapshot = Consistent Global State**

 A consistent snapshot is a global system state which is consistent with all local views.

## Global System State (for schedule S)

- A vector of intermediate states (in S) of all nodes and a description of the messages currently in transit
  - Remark: If nodes keep logs of messages sent and received, the local states contain the information about messages in transit.

#### **Consistent Snapshot**

• A global system state which is an intermediate global state for some causal shuffle of S (consistent with all local views)

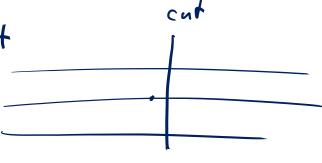
# **Consistent Snapshot**

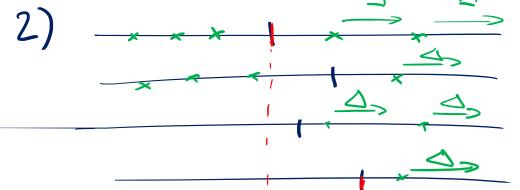


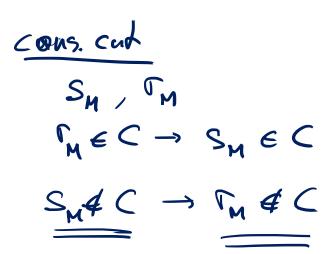
Claim: A global system state is a consistent snapshot if and only if it corresponds to the node states of some consistent cut C.

Cous. suapshot = consistent out

1) inbrm. State of all processes -> cut
consistent V







# Computing a Consistent Snapshot



#### **Using Logical Clocks**

• Assume that each event e has a clock value  $\underline{\tau(e)}$  such that for two events e, e',

$$e \Rightarrow_S e' \rightarrow \tau(e) < \tau(e')$$

• Given  $\tau$ , define  $\underline{\underline{C(\tau)}}$  as the set of events e with  $\underline{\tau(e) \leq \tau_0}$ 

**Claim:**  $\forall \tau \geq 0$ :  $C(\tau)$  is a consistent cut.

**Remark:** Not always clear how to choose  $au_0$ 

- $\tau_0$  large: not clear how long it takes until snapshot is computed
- $\tau_0$  small: snapshot is "less up-to-date"



Goals: Compute a consistent snapshot in a running system

#### **Assumptions:**

- Does not require logical clocks
- Channels are assumed to have FIFO property
- · No failures (no nocle failures, no msg. (osses)
- Network is (strongly) connected
- Any node can issue a new snapshot

# Remark: The FIFO property can always be guaranteed

- sender locally numbers messages on each outgoing channel
- messages with smaller numbers have to be processed before messages with larger numbers
- works as long as messages are not lost



#### **Overview:**

- w w
- Assume that node s initiates the snapshot computation
- The times for recording the state at different nodes is determined by sending around marker messages
- When receiving the first marker message, a node records its state and sends marker messages to all (outgoing) neighbors
- On each incoming channel, the set of messages which are received between recording the state and receiving the marker message (on this channel) are in transit in the snapshot.
- After receiving a marker message on all incoming channels, a nodes has finished its part of the snapshot computation



Initially: Node s records its state u is small worker way. When node u receives a marker message from node v:

if u has not recorded its state then u records its state

set of msg. in transit from v to u is empty u starts recording messages on all other incoming channels else

the set of msg. in transit from v to u is the set of recorded msg. since starting to record msg. on the channel

## (Immediately) after node u records its state:

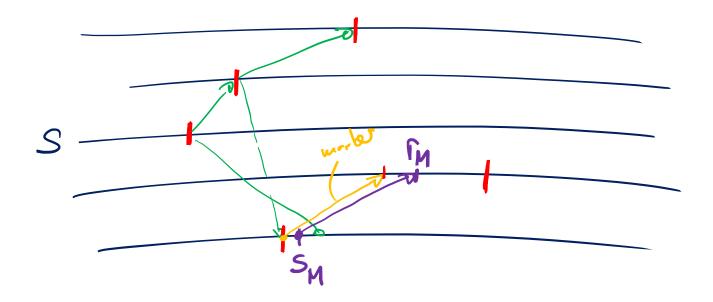
Node u sends marker msg. on all outgoing channels

before sending any other message on those channels



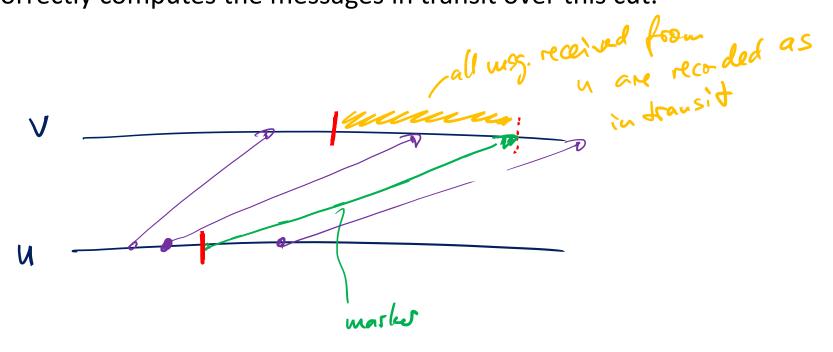
**Theorem:** The Chandy-Lamport algorithm computes a consistent cut and it correctly computes the messages in transit over this cut.

Consisked Cat





**Theorem:** The Chandy-Lamport algorithm computes a consistent cut and it correctly computes the messages in transit over this cut.



# **Applications of Consistent Snapshots**



#### **Testing Stable System Properties**

- A stable property is a property which once true, remains true
- More formally: a predicate P on global configurations such that if P is true for some configuration C, P also holds for all configurations which can be reached from C

#### **Testing a stable property:**

test whether property holds for a consistent snapshot

#### Safety: Only evaluates to true if the property holds

the current state is reachable from every consistent snapshot state

#### Liveness: If the property holds, it will eventually be detected

initiating a snapshot (using Chandy-Lamport) leads to snapshot configuration which is reachable from the current configuration

# **Applications of Consistent Snapshots**



#### **Distributed Garbage Collection**

- Erase objects (e.g., variables stored at some node(s)) to which no reference exists any more
- References can be at other nodes, in messages in transit, ...
- "No reference to object x" is a stable system property

#### **Distributed Deadlock Detection**

- Two processes/nodes wait for each other
- Deadlock is also a stable property

#### **Distributed Termination Detection**

- "Distributed computation has terminated" is a stable property
- Note, need also see messages in transit