



Chapter 10 Parallel Algorithms

Algorithm Theory WS 2018/19

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Sequential Algorithms

Classical Algorithm Design:

• One machine/CPU/process/... doing a computation

RAM (Random Access Machine):

- Basic standard model
- Unit cost basic operations
- Unit cost access to all memory cells

Sequential Algorithm / Program:

 Sequence of operations (executed one after the other)



Parallel and Distributed Algorithms



Today's computers/systems are not sequential:

- Even cell phones have several cores
- Future systems will be highly parallel on many levels
- This also requires appropriate algorithmic techniques

Goals, Scenarios, Challenges:

- Exploit parallelism to speed up computations
- Shared resources such as memory, bandwidth, ...
- Increase reliability by adding redundancy
- Solve tasks in inherently decentralized environments

Parallel and Distributed Systems



- Many different forms
- Processors/computers/machines/... communicate and share data through
 - Shared memory or message passing
- Computation and communication can be
 - Synchronous or asynchronous
- Many possible topologies for message passing
- Depending on system, various types of faults

Challenges



Algorithmic and theoretical challenges:

- How to parallelize computations
- Scheduling (which machine does what)
- Load balancing
- Fault tolerance
- Coordination / consistency
- Decentralized state
- Asynchrony
- Bounded bandwidth / properties of comm. channels

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Models

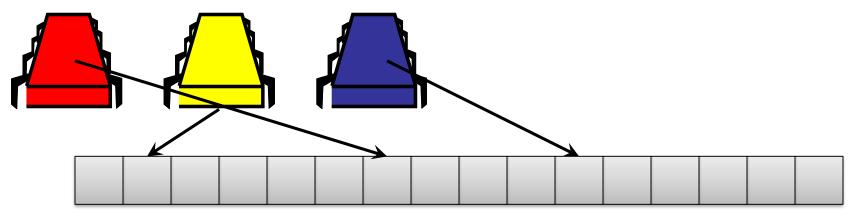


- A large variety of models, e.g.:
- **PRAM** (Parallel Random Access Machine)
 - Classical model for parallel computations
- Shared Memory
 - Classical model to study coordination / agreement problems, distributed data structures, ...
- Message Passing (fully connected topology)
 - Closely related to shared memory models
- Message Passing in **Networks**
 - Decentralized computations, large parallel machines, comes in various flavors...
- Computations in large clusters of powerful individual machines: Massively Parallel Computations (MPC)

PRAM



- Parallel version of RAM model
- *p* processors, shared random access memory



- Basic operations / access to shared memory cost 1
- Processor operations are synchronized
- Focus on parallelizing computation rather than cost of communication, locality, faults, asynchrony, ...

Other Parallel Models

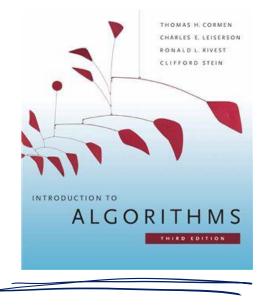


- **Message passing:** Fully connected network, local memory and information exchange using messages
- **Dynamic Multithreaded Algorithms:** Simple parallel programming paradigm
 - E.g., used in Cormen, Leiserson, Rivest, Stein (CLRS)

FIB
$$(n)$$

1 if $n < 2$
2 then return n
3 $x \leftarrow \text{spawn FIB}(n-1)$
4 $y \leftarrow \text{spawn FIB}(n-2)$
5 sync
6 meture $(n + y)$

6 return (x+y)



Parallel Computations

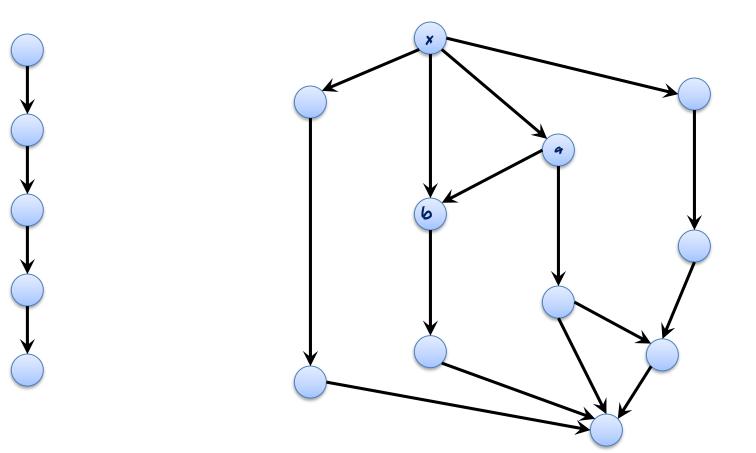


Sequential Computation:

• Sequence of operations

Parallel Computation:

• Directed Acyclic Graph (DAG)



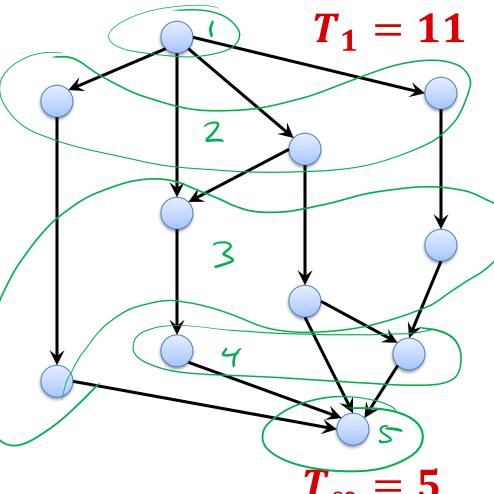
Parallel Computations



 T_p : time to perform comp. with p procs

- T₁: work (total # operations)
 - Time when doing the computation sequentially
- T_∞ : critical path / span
 - Time when parallelizing as much as possible
- Lower Bounds:

$$T_p \geq \frac{T_1}{p}$$
,



 $T_p \geq T_c$