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## Algorithms and Data Structures Winter Term 2020/2021 Exercise Sheet 4

## Exercise 1: Hashing - Collision Resolution with Open Addressing

(a) Let  $h(s,j) := h_1(s) - 2j \mod m$  and let  $h_1(x) = x + 2 \mod m$ . Insert the keys 51, 13, 21, 30, 23, 72 into the hash table of size m = 7 using linear probing for collision resolution (the table should show the final state).

0	1	2	3	4	5	6

(b) Let  $h(s, j) := h_1(s) + j \cdot h_2(s) \mod m$  and let  $h_1(x) = x \mod m$  and  $h_2(x) = 1 + (x \mod (m-1))$ . Insert the keys 28, 59, 47, 13, 39, 69, 12 into the hash table of size m = 11 using the double hashing probing technique for collision resolution. The hash table below should show the final state.

0	1	2	3	4	5	6	7	8	9	10

## Exercise 2: Application of Hashtables

Consider the following algorithm:

## Algorithm 1 algorithm

 $\triangleright$  Input: Array A of length n with integer entries

```
1: for i = 1 to n - 1 do
2: for j = 0 to i - 1 do
3: for k = 0 to n - 1 do
4: if |A[i] - A[j]| = A[k] then
5: return true
```

- 6: return false
- (a) Describe what algorithm computes and analyse its asymptotical runtime.
- (b) Describe a different algorithm  $\mathcal{B}$  for this problem (i.e.,  $\mathcal{B}(A) = \mathtt{algorithm}(A)$  for each input A) which uses hashing and takes time  $\mathcal{O}(n^2)$ .
  - You may assume that inserting and finding keys in a hash table needs  $\mathcal{O}(1)$  if  $\alpha = \mathcal{O}(1)$  ( $\alpha$  is the load of the table).
- (c) Describe another algorithm for this problem without using hashing which takes time  $\mathcal{O}(n^2 \log n)$ .