

Theoretical Computer Science Bridging Course Introduction / General Info

Winter Term 2020/21 Fabian Kuhn

About the Course



Topics

- Foundations of theoretical computer science
- Introduction to logic

No lectures

There are recordings which you are supposed to watch

Exercises

- There will be weekly exercises which you should do
 - Doing the exercises is not mandatory, but highly recommended

Exam

- A 30 min oral exam at the end of the term
 - Details will be published on the course web page a.s.a.p.

About the course



What is the purpose of the course? Who is it targeted to?

- The course is for incoming M.Sc. students who do not have the necessary theory background required by the M.Sc. program.
 - E.g., students who did not study computer science or students from more applied schools, ...

Website



All necessary information about the course will be published on

http://ac.informatik.uni-freiburg.de/teaching/ws20_21/tcs-bridging.php

- Or go to my group's website: http://ac.informatik.uni-freiburg.de
- Then follow teaching winter term 2020/21 TCS bridging course
- Please check the website for
 - Recordings and slides
 - Exercises and sample solutions
 - Pointers to additional literature
 (e.g., written lecture notes from an older version of this lecture)
 - Information about the exam
 - **–** ...

Zulip



- Zulip is a group chat / forum (https://zulip.com)
- We have our own Zulip server, which we will use for online discussions regarding our lectures.
 - In addition to the website, please check Zulip for announcements, etc.
 - Use Zulip to discuss questions regarding the lecture / exercises.
- Please send an email to the tutor in order to be added to our zulip server.
 - Email address: <u>salwa.faour@cs.uni-freiburg.de</u>

Exercises



There will be weekly exercise sheets:

- Exercise sheets are published at the latest on Monday on the website
- Exercises are due after one week on the coming Monday before the exercise tutorial
 - If you want corrections / comments from your tutor
 - Hand in your exercises via <u>email</u> to your tutor.
- If you work in a group, the group needs to hand in one solution
 - Make sure that all students participate in solving & writing equally!
- After getting back your exercises, you can (virtually) meet and discuss the exercises with your tutor OR on Zulip
 - On Tuesdays or if additional help is necessary on request

Exercise Tutorials



Assistant / Tutor for the course:

Salwa Faour, <u>salwa.faour@cs.uni-freiburg.de</u>

Weekly Tutorials:

- There is a weekly online tutorial every Monday from 12:15 – 14:00 via Zoom.
- The Zoom link and other related details are provided on this course website.
- In the tutorial, we discuss the upcoming exercise sheet and your solutions of the last exercise sheet
 - You are required to actively participate in the tutorials and ask questions.
- Also ask your tutor if you have any questions!

Exercises



The exercises are the most important part of the course!

- To pass the exam, it is important that you do the exercises
- If you feel comfortable with all the exercises, you should also be able to pass the exam

- When working in groups, make sure that you all participate in solving the questions and in writing the solutions!
 - You should all be able to explain your solutions to your tutor.

Course Topics



Foundations of Theoretical Computer Science

- Automata theory
- Formal languages, grammars
- Turing machines
- Decidability
- Computational complexity

Introduction to Logic

- Propositional logic
- First order logic

Purpose of the Course



Goal: Understand the fundamental capabilities and limitations of computers

- What does it mean to "compute"?
 - Automata theory
- What can be computed?
 - Theory on computability/decidability
- What can be computed efficiently?
 - Computational complexity

Meaning of "Computing"



Mathematical Models

•	Turing machines	1930s
•	Turing machines	1930

Finite state automata 1940s

Formal grammars 1950s

Practical Aspects

• Compute architectures 1970	•	Compute	architectures	1970s
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Programming languages 1970s

Compilers 1970s

Is My Function Computable?



Write an algorithm / computer program to compute it

- Can it compute the right answer for every instance?
- Does it always give an answer (in finite time)?
- Then you are done.

Otherwise, there are two options

- There is an algorithm, but you don't know it
- There is no algorithm → the problem is unsolvable

Formally proving computability is sometimes hard!

But you will learn how to approach this...

Is My Function Computable?



- Many "known" problems are solvable
 - Sorting, searching, knapsack, TSP, ...
- Some problems are not solvable
 - Halting problem
 - Gödel incompleteness theorem
- Don't try to solve unsolvable problems!

Can I Compute My Function Efficiently?



- Some problems are "easy"
 - Can we formally define what this means?
- Complexity theory is about this
 - Complexity classes, tools for checking membership
- It is important to know how hard a problem is!

Feasible problems:

- E.g., sorting, linear programming, LZW compression, primality testing, ...
- Time to solve is polynomial in the size of the input

Problems that are considered infeasible

- Some scheduling problems, knapsack, TSP, graph coloring, ...
- Important open question: "Is P = NP"?

Unfeasible problems

Time exponential in input, e.g., quantified Boolean formula

Questions?



Warming up

for TCS Bridging Course

• Mathematical objects, tools, notions:

- Sets
- Sequences
- Functions
- Graphs
- Strings and languages
- Types of Proof:
- By construction
- By contradiction
- By induction
- By counterexample

- The alphabet set $\Sigma = \{a, c, n, o, r\}$
- A={ no, corona}
- B= {no, corona, roar, ac}
- Is $A \subseteq B$?
- Is $B \subseteq A$?
- A ∪ *B*?
- A ∩ B?
- •B\A?
- •A\B?

For any two sets A and B,

$$A \Delta B = \emptyset \Leftrightarrow A = B$$

Proof

$$\Rightarrow$$
): A \triangle B = (A\B) \cup (B\A)= \emptyset

$$(A\B)=\emptyset$$
 and $(B\A)=\emptyset$

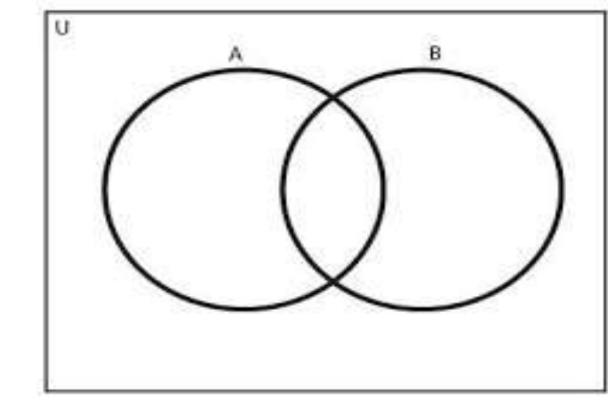






 $B \subseteq A$

$$A=B$$



• Mathematical objects, tools, notions:

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A 10 Year Old Discovered This Famous Formula

$$1+2+...+n=\frac{n(n+1)}{2}$$



Induction

• Goal: for an integer $n \ge 0$, use mathematical induction to prove a statement holds true for all values of n.

2 STEPS:

• Base case :

prove the statement true for n = 0

• Induction step:

assume the statement holds for any given case n = k, where $k \ge 0$ and use this assumption to prove the statement true for n = k + 1.

- Use proof by induction to prove
- $1+2+...+n=\frac{n(n+1)}{2}$, for $n \ge 1$
- Base step: for n=1, we have $\frac{1(1+1)}{2} = 1$
- Inductive hypothesis: assume for any case n=k holds, where k is some integer $k \ge 1$

i.e. $1+2+...+k = \frac{k(k+1)}{2}$, where k is some integer $k \ge 1$

Now, let's prove the statement true for n=k+1

i.e.
$$1+2+...+(k+1)=\frac{(k+1)(k+2)}{2}$$
 (is it true?)

$$1+2+...k+(k+1)=\frac{k(k+1)}{2}+(k+1)=\frac{k(k+1)+2(k+1)}{2}=\frac{(k+1)(k+2)}{2}$$
 (Yes!)

• Mathematical objects, tools, notions:

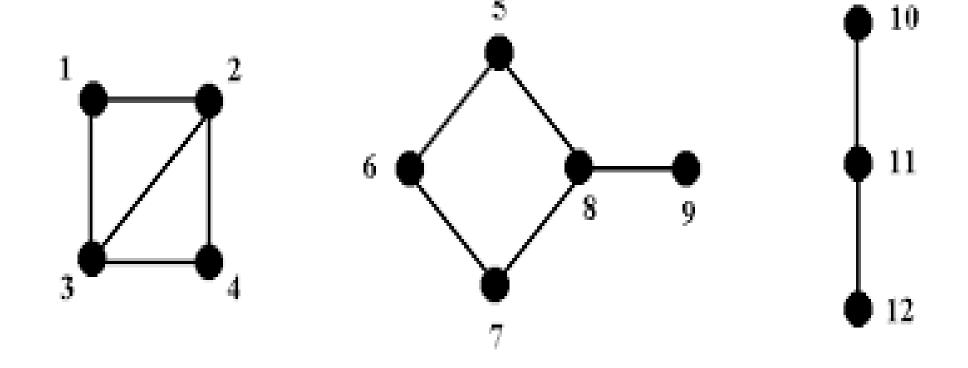
- Sets
- Sequences
- Functions



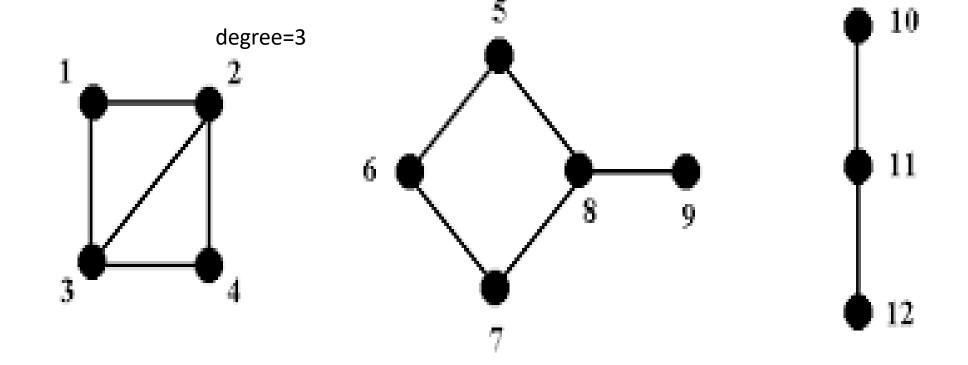
- Graphs
- Strings and languages
- Types of Proof:
- By construction
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- By counterexample

Graphs

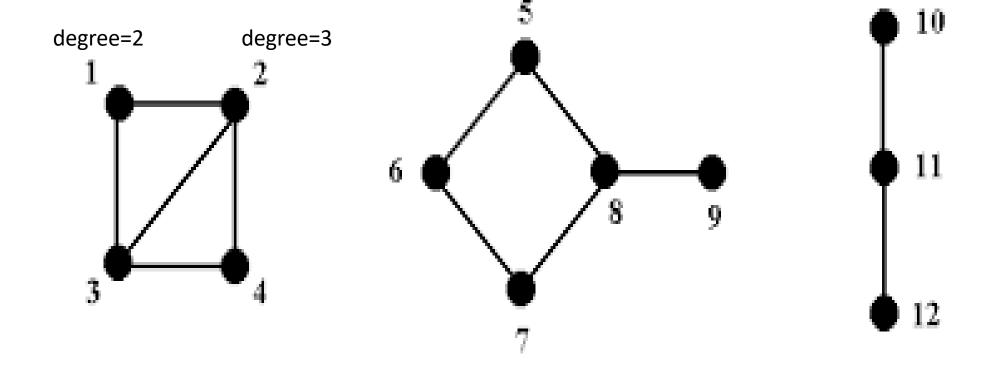
We write G=(V,E).



Graphs



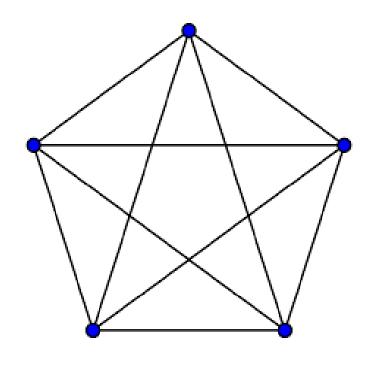
Graphs



How many edges in a complete graph on **n** vertices?

n(n-1)/2 edges!

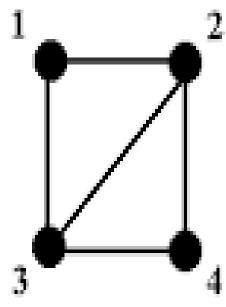
Don't count each edge twice



How many edges are there in a simple graph G= (V, E) ?

• $\sum_{v \in V} degree(v) = 2 |E|$ (Handshaking Lemma)

• Each edge contributes 2 to the sum on the left.



Can you?

• Draw a graph on 5 nodes such that each node is of degree 3.

Can you?

Draw a graph on 5 nodes such that each node is of degree 3

• Solution: you can't!

• Sum of all degrees= 5 x 3= 15

• See you Next Week!