



Algorithms and Data Structures Summer Term 2019 Exercise Sheet 5

Exercise 1: Priority Queues

Consider the following priority queue stored in an array:

$$H = [(3, L), (10, D), (8, E), (12, C), (13, B), (23, R), (9, F), (17, S), (14, M)]$$

Execute the following operations on H : $H.insert((7, N))$, $H.deleteMin()$, $H.changeKey((13, B), 9)$. Write down H after each operation including the repairing process. It may help if you draw H as a binary tree.

Exercise 2: Amortized Analysis

Consider the data structure **stack** in which elements can be stored in a ‘last in first out’ manner. For a stack S we have the following operations:

- $S.push(x)$ puts element x onto S .
- $S.pop()$ deletes the topmost element of S . Calling pop on an empty stack generates an error.
- $S.multipop(k)$ removes the k top objects of S , popping the entire stack if S contains fewer than k objects.

Assume the costs of $S.push(x)$ and $S.pop()$ are 1 and the cost of $S.multipop(k)$ is $\min(k, s)$ where s is the current number of elements in S .

Use the bank account paradigm to show that we can assign all three operations constant amortized costs.