Algorithms and Datastructures Runtime analysis Minsort / Heapsort, Induction

Albert-Ludwigs-Universität Freiburg

### Prof. Dr. Rolf Backofen

Bioinformatics Group / Department of Computer Science Algorithms and Datastructures, October 2018



### Structure

# UNI FREIBURG

### Algorithms and Datastructures

Structure Links

Organisation

- Daphne
- Forum
- Checkstyle
- Unit Tests
- Version management
- Jenkins

### Sorting

Minsort Heapsort



### Topics of the Lecture:

- Algorithms and Data Structures Efficient data handling and processing ... for problems that occur in practical **any** larger program / project
- **Datastructure ÷** Representation of data on computer

### Example 1: Sorting



### Figure: Sorting with Minsort

### **Example 2: Navigation**

- Datastructures: How to represent the map as data?
- Algorithms: How to find the shortest / fastest way?



### Figure: Navigationplan © OpenStreetMap

# UNI FREIBURG

### Content of the Lecture 1 / 2

# UNI FREIBURG

### General:

Most of you had a lecture on basic progamming ...

### performance was not an issue

### Here it is going to be:

- How fast is our program?
- 2 How can we make it faster?
- 3 How can we proof that it will always be that fast?

### Important issues:

- Most of the time: application runtime
- Sometimes also: resource / space consumption

### Content of the Lecture 2 / 2

# UNI FREIBURG

### Algorithms:

- Sorting
- Dynamic Arrays
- Associative Arrays
- Hashing
- Edit distance

### Mathematics:

- Runtime analysis
- *O*-Notation

- Priority Queue
- Linked Lists
- Pathfinding / Dijkstra Algorithm
- Search Trees

Proof of correctness

### After the lecture ...

■ ... you should be able to understand the joke



### Figure: Comic @ xkcd/835

### Hopefully your parents will still invite you

October 2018

**DRG** 

a





JRG

### Homepage:

- Exercise sheets
- Lectures
- Materials

### Link to Homepage





### Lecture:

- Tuesday, 12:00 14:00, HS 00 006, Build. 082
- Recordings of the lecture will be uploaded to the webpage

### Exercises:

- One exercise sheet per week
- Submission / Correction / Assistance online
- Tutorial: (if needed) Wednesday, 13:00-14:00 - HS 00 006, Build. 082

### Exam:

 Planned: Sa. 23th March 2019, 10:00-12:00, Build. 101, Lec. theater 026 & 036

### Organisation 2 / 5



### Exercises:

- 80% practical, 20% theoretical
- We expect everyone to solve every exercise sheet

### Exam:

- 50% of all points from the exercise sheets are needed
- Content of exam: whole lecture **and all exercises**

### Organisation - Exercises 3 / 5



### Exercises:

- Tutors: Tim Maffenbeier, Till Steinmann, Tobias Faller
- Coordinators: Michael Uhl, Florian Eggenhofer and Björn Grüning
- Deadline: ESE: 1 week, IEMS: none

### Organisation - Exercises 3 / 5

# 

### Exercises:

- Post questions into the forum (link later)
- Submission via "commit" through svn and Daphne
- Feedback one week after deadline through "update" (svn)
- Unit test / checkstyle via Jenkins

### Organisation - Exercises 4 / 5

### **Exercises - Points:**

- Practical:
  - 60% functionality
  - 20% tests
  - 20% documentation, Checkstyle, etc.
  - Program is not running  $\Rightarrow$  0 points
- Theoretical (mathematical proof):
  - 40% general idea / approach
  - 60% clean / complete

BUR

### Organisation 5 / 5



### Effort:

- 4 ECTS (ESE), 6 ECTS (IEMS)
- 120 / 180 working hours per semester
- 14 Lectures each 6h / 8h + exam
- 4h / 6h per exercise sheet (one per week)

Daphne



### Daphne:

- Provides the following information:
  - Name / contact information of your tutor
  - Download of / info needed for exercise sheets
  - Collected points of all exercise sheets
  - Links to:
    - Coding standards
    - 2 Build system
    - 3 The other systems

### Link: Daphne





### Forum:

- Please don't hesitate to ask if something is unclear
- Ask in the forum and not separate. Others might also be interested in the answer
- The tutors or the coordinators will reply as soon as possible
- Link: Forum



### Checkstyle / Linting (flake8):

- Installation: python3 -m pip install flake8
- Check file: python3 -m flake8 path/to/files/\*.py
- Link: flake8





### Why unit tests?

- A non-trivial method without a unit test is probably wrong
- 2 Simplifies debugging
- 3 We and you can automatically check correctness of code

### What is a good unit test?

- Unit test checks desired output for a given input
- At least one typical input
- At least one critical case
  - E.g. double occurrence of a value in sorting

### Unit Tests doctest

Testing (doctest):

```
def subtract_one(n):
    """Subtracts 1 from n
    >>> subtract_one(5)
    4
    >>> subtract_one(3)
    2
    """
    return n-1
```

if \_\_name\_\_ == "\_\_main\_\_":
 print("2 - 1 = %d" % subtract\_one(2))

- Tests are contained in docstrings
- Module doctest runs them
- Run check with: python3 -m doctest path/to/files/\*.py -v

BURG



### Version management (subversion):

- Keeps a history of code changes
- Initialize / update directory: svn checkout <URL>
- Add files / folders: **svn** add <file> --all
- Create snapshot: svn commit -m "<Your Message>" Data is uploaded to Jenkins automatically
- Link: Subversion

Jenkins



### Jenkins:

- Provides our build system
- You can check if your uploded code runs
  - Especially whether all unit test pass
  - And if **checkstyle** (flake8) is statisfied
- Will be shown in the first exercise
- Link: Jenkins

### Sorting 1 / 2



### Problem:

- Input: *n* elements  $x_1, \ldots, x_n$
- Transitive operator "<" which returns true if the left value is smaller than the right one

Transitivity: x < y,  $y < z \rightarrow x < z$ 

Output:  $x_1, \ldots, x_n$  sorted with operator

### Example

Input: 14, 4, 32, 19, 8, 44, 65 Output:





### Why do we need sorting?

Nearly every program needs a sorting algorithm

### Examples:

- Index of a search engine
- Listing filesystem in explorer / finder
- (Music) library
- Highscore list

### Minsort - Algorithm



### Informal description:

- Find the minimum and switch the value with the first position
- Find the minimum and switch the value with the second position



Figure: Minsort

. . .

### Minsort - Algorithm

### Minsort in Python:

```
def minsort(lst):
    for i in range(0, len(lst)-1):
        minimum = i
        for j in range(i+1, len(lst)):
            if lst[j] < lst[minimum]:</pre>
                 minimum = j
        if minimum != i:
             |st[i], |st[minimum] = 
                 lst[minimum], lst[i]
```

### return Ist

**IBUR** 

### How long does our program run?

### Table: Runtime for Minsort

	п	Runtime / ms
<ul> <li>We test it for different input sizes</li> <li>Observation: It is going to be "disproportionately" slower the more numbers are being sorted</li> </ul>	$2  imes 10^3$	5.24
	$4  imes 10^3$	16.92
	$6  imes 10^3$	39.11
	$8 imes 10^3$	67.80
	$10 imes10^3$	105.50
	$12  imes 10^3$	150.38
	$14 imes10^3$	204.00
	$16 imes10^3$	265.98
	$18  imes 10^3$	334.94

### MinSort - Runtime

### How long does our program run?

- We test it for different input sizes
- Observation:

It is going to be "disproportionately" slower the more numbers are being sorted



### Figure: Runtime of Minsort

### MinSort - Runtime

### **Runtime analysis:**

- Minsort runtime depicted in a diagram
  - That is what you should do in the first exercise sheet
- We observe:
  - The runtime grows faster than linear
  - With double the input size we need four times the time



### Figure: Runtime of Minsort





### Heapsort:

- The principle stays the same
- Better structure for finding the smallest element quicker

### Binary heap:

- Preferably a complete binary tree
- Heap property: Each child is smaller (larger) than the parent element

### Min heap:

- Heap property: Each child is smaller (larger) than the parent element
- A valid heap fulfills the property at each node



### Heapsort - Algorithm 3 / 10

### How to save the heap?

- We number all nodes from top to bottom and left to right starting at 0
  - The children of node *i* are 2*i* + 1 and 2*i* + 2
  - The parent node of node *i* is floor  $\left(\frac{i-1}{2}\right)$





### Repairing after taking the smallest element: heap.pop()

- Remove the smallest element (root node)
- Replace the root with the last node
- Sift the new root node down until the heap property is satisfied



q

17

## HeapSort - Algorithm 5 / 10

### Heapsort:

- Organize the n elements as heap
- While the heap still contains elements
  - Take the smallest element
  - Move the last node to the root
  - Repair the heap as described
- Output: 4, 5, …



11

q







### Creating a heap:

- This operation is called heapify
- The *n* elements are already stored in an array
- Interpret the array as binary heap where the heap property is not yet satisfied
- We repair the heap from bottom up (in layers) with sift

### Heapsort - Algorithm 7 / 10



Figure: Heapify lower layer

**D**RG

### Heapsort - Algorithm 8 / 10



Figure: Heapify upper layer

22

### Heapsort - Algorithm 9 / 10





### Finding the minimum is intuitive:

- Minsort: Iterate through all non-sorted elements
- Heapsort: Finding the minimum is trivial (concept) Just take the root of the heap

### Removing the minimum in Heapsort:

- Repair the heap and restore the heap property
  - We don't have to repair the whole heap
- More of this in the next lecture

BURG

### Further Literature



### Course literature

[CRL01] Thomas H. Cormen, Ronald L. Rivest, and Charles E. Leiserson.
Introduction to Algorithms. MIT Press, Cambridge, Mass, 2001.
[MS08] Kurt Mehlhorn and Peter Sanders. Algorithms and Data Structures. Springer, Berlin, 2008. https://people.mpi-inf.mpg.de/~mehlhorn/ ftp/Mehlhorn-Sanders-Toolbox.pdf.

### Further Literature



### Sorting

[Wika] Wikipedia - Heapsort https://en.wikipedia.org/wiki/Heapsort [Wikb] Wikipedia - Selectionsort

https://de.wikipedia.org/wiki/Selectionsort



### Subversion

[Apa] Apache Subversion https://subversion.apache.org/